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Forecast Accuracy and Safety Stock Strategies^o



White Paper

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Forecast Accuracy - Abstract



Accurate and timely demand plans are a vital component of an effective supply chain.

- Forecast accuracy at the primitive SKU level is critical for proper allocation of supply chain resources.
- Inaccurate demand forecasts often would result in supply imbalances when it comes to meeting customer demand.

In this white paper, we will discuss the process of measuring forecast accuracy, the pros and cons of different accuracy metrics, and the time-lag with which accuracy should be measured. We will also discuss a method to identify and track forecast bias.

Demand Plan



- ∅ Demand Plan is a statement of expected future demand that is derived using a statistical forecast plus customer intelligence.
- ∅ Demand Plans need to be
 - ∅ Accurate
 - ∅ Timely
 - ∅ In relevant detail
 - ∅ Covering the appropriate time horizon
- ∅ *What is different between Long-term and Short-term Planning?*

Short-term Planning



- Ø Critical for tactical planning
- Ø Limited flexibility to reschedule resources

So Make or Break it!

Ø Inaccurate forecast means

- Lost sale
- Lost customer
- Excess inventory
- Other inefficiencies

Long-term Forecasts



- Ø Market or economy-oriented
- Ø Useful for
 - Capacity Planning
 - Setting Strategic initiatives
- Ø More flexibility to change and err
- Ø Accuracy at an aggregate or macro level is more important
- Ø **So mix matters less in Long-term forecasting!**

Right amount, wrong SKU!



	<u>SKU A</u>	<u>SKU B</u>	<u>Total</u>
Forecast	75	25	100
Actual	25	75	100
Accuracy	0%	0%	100%

Forecast Error



Ø Forecast Error is the deviation of the Actual from the forecasted quantity

- Error = absolute value of {(Actual – Forecast)}
- Error (%) = $|A - F| / A$

Ø Deviation vs. Direction

- The first is the magnitude of the Error
- The second implies bias, if persistent

Forecast Accuracy



- Ø Forecast Accuracy is a measure of how close the Actual Demand is to the forecasted quantity.
 - Forecast Accuracy is the converse of Error
 - $\text{Accuracy (\%)} = 1 - \text{Error (\%)}$
- Ø However we truncate the Impact of Large Forecast Errors at 100%.
- Ø More formally
 - $\text{Actual} = \text{Forecast} \Rightarrow 100\% \text{ Accuracy}$
 - $\text{Error} > 100\% \Rightarrow 0\% \text{ Accuracy}$
 - We constrain Accuracy to be between 0 and 100%
- Ø More Rigorously,
 - $\text{Accuracy} = \text{maximum of } (1 - \text{Error}, 0)$

Example (continued...)



	<u>SKU A</u>	<u>SKU B</u>	<u>SKU X</u>	<u>SKU Y</u>
Forecast	75	0	25	75
Actual	25	50	75	74
Error	50	50	50	1
Error (%)	200%	100%	67%	1%
Accuracy (%)	0%	0%	33%	99%



How do you measure value chain performance? Find out at the DemandPlanning.Net [metrics workshop!](#)

CALCULATION METHODOLOGY

- Ø How to calculate a performance measure for forecast accuracy?
- Ø How do we aggregate errors across products and customers?
- Ø What are the different error measurements available?
- Ø How do you define the Mean Absolute Percent Error?
- Ø What is the weighted MAPE?

Aggregating Errors



To compute one metric of accuracy across a group of items, we need to calculate an Average Error

Ø Simple but Intuitive Method

- Add all the absolute errors across all items
- Divide the above by the total actual quantity
- Define the average error as Sum of all Errors divided by the sum of Actual shipments

Ø This is known as MAPE or

Mean Absolute Percentage Error!!!!

Example of MAPE calculation



	<u>Sku A</u>	<u>SKU B</u>	<u>SKU X</u>	<u>SKU Y</u>	<u>Total</u>
Forecast	75	0	25	75	175
Actual	25	50	75	74	224
Error	50	50	50	1	151
Error (%)	200%	100%	67%	1%	67%
Accuracy (%)	0%	0%	33%	99%	33%

Different ways to err!



Ø Mean Percent Error

Ø Mean Absolute Percent Error or MAPE

Ø Mean Squared Error

Ø Root Mean Squared Error

Different ways to err!



- Ø Mean Percent Error is an Average of the Absolute Percentage Error. Very rarely used!
- Ø Mean Absolute Percent Error is the Sum of Absolute errors divided by the Sum of the Actuals
 - $MAPE = \frac{\sum |(A-F)|}{\sum A}$
 - MAPE can also be construed as the Average Absolute Error divided by the Average Actual quantity
 - Most widely used measure
- Ø Mean Squared Error is the Average of the sum-squared errors. Since we use the root of such average, this is also known as RMSE
 - $RMSE = \sqrt{[(A-F)^2 / N]}$

Illustration of Error Metrics



	Forecast	Actual	Error	Abs. Error	Pct. Error	Sqrd. Error
Sku A	3	1	-2	2	200%	4
Sku B	0	50	50	50	100%	2,500
Sku X	25	75	50	50	67%	2,500
Sku Y	75	74	-1	1	1%	1
Sku Z	100	75	-25	25	33%	625
Total	203	275	72	128		5,630
Average	40.6	55	14.4	25.6	80%	1,126
					with A	w/o Sku A
	Mean Percent Error =				80%	50%
	Mean Absolute Percent Error =				47%	46%
	Root Mean Squared Error =				34	38
	RMSE as % of Actuals =				61%	55%

Why MAPE?



Ø MPE

- very unstable
- will be skewed by small values
- In the Example, Sku A drives most of the Error.

Ø RMSE

- Rigorous Error measure
- Not as easy as MAPE

Ø MAPE is simple and elegant while robust as a computational measure!

MAPES!!



- Ø The simple MAPE is volume-weighted rather than value weighted.
 - Assumes the absolute error on each item is equally important.
 - Large error on a low-value item or C item can unfairly skew the overall error.
- Ø To overcome this, MAPE can be value weighted either by standard cost or list price
 - High-value items will influence the overall error

WMAPE



Ø Weighted Mape or Value weighted Mape

- $WMAPE = \frac{\sum (w^* |(A-F)|)}{\sum (w^* A)}$
- Both Error and Actuals are weighted
- The weight can even be a subjective measure based on criticality of the item.

Ø High-value items will influence the overall error

Ø Highly correlated with safety stock requirements

Ø Very useful in setting safety stock strategies



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LAG AND BIAS

- Ø What is forecast bias?
- Ø How to measure forecast bias?
- Ø What is the forecast lag for evaluating forecasts?
- Ø How do you determine forecast lags?

Absolute vs. Arithmetic!



	Forecast	Actual	Error	Abs. Error	Pct. Error
Sku A	3	1	-2	2	200%
Sku B	0	50	50	50	100%
Sku X	25	75	50	50	67%
Sku Y	75	74	-1	1	1%
Sku Z	100	75	-25	25	33%
Total	203	275	72	128	
Average	40.6	55	14.4	25.6	80%
	Mean Absolute Percent Error =				47%
	Absolute Accuracy (%)				53%
	Arithmetic Accuracy				135%

Absolute vs. Arithmetic



Ø Absolute accuracy is the converse of MAPE.

- A 47% MAPE implies accuracy of 53%.

Ø Arithmetic Accuracy is a measure of total business performance regardless of the mix issues

- Defined as a simple quotient of Actual vs. Forecast
- Directionally offsetting errors result in accuracy close to 100%
- Arithmetic Accuracy is also known as Forecast Attainment.

Lead vs. Lag



- Ø Setting measurement standards will be influenced by
 - Production Lead time
 - Batch Size
- Ø Production Lead time dictates the Forecast Lag to be used in computing accuracy
 - Longer the lead time, larger is the forecast Lag
 - Larger the Lag, lower the forecast accuracy

Lag Analysis



	March	April	May	June	July
March	125	130	175	210	225
Lag	0	1	2	3	4
April		135	185	220	235
Lag		0	1	2	3
May			170	225	225
Lag			0	1	2
Actuals	128	135	172	225	

Lag 2
Forecast

Evolution of
forecast

Forecast Bias



Bias is the tendency for error to be persistent in one direction. Most bias can be classified into one of two main categories:

Ø **Forecaster bias** occurs when error is in one direction for all items.

Ø **Business Process Bias** occurs when error is in one direction for specific items over a period of time.

Forecast Bias – Case 1



	Forecast	Actual	Error	Abs. Error	Pct. Error	Accuracy
Sku A	3	1	-2	2	200%	0%
Sku B	50	25	-25	25	100%	0%
Sku X	75	25	-50	50	200%	0%
Sku Y	75	74	-1	1	1%	99%
Sku Z	100	75	-25	25	33%	67%
Total	303	200	-103	103	52%	48%
Average	60.6	40	-20.6	20.6		
	Absolute Accuracy				48%	
	Arithmetic Accuracy				66%	

Type 1 Bias



∅ This is a subjective bias. Occurs due to human intervention (often erroneous) to build unnecessary forecast safeguards.

Examples:

- Increase forecast to match Division Goal
- Adjust forecast to reflect the best case volume scenario in response to a promotion
- Building a forecast component to reflect production uncertainty (in effect, doubling the safety stock)
- Organization's natural tendency to over-forecast due to high visibility of product outs compared to excess inventory

∅ This bias results in

- Increased inventories and
- Higher risk of obsolescence.

Forecast Bias – Case 2



	Arithmetic Accuracy				May	Bias
	Jan	Feb	Mar	Apr		
SKU A	110%	118%	121%	101%	112%	+
SKU B	88%	92%	90%	81%	88%	-
SKU X	95%	104%	101%	100%	97%	No
SKU Y	65%	135%	70%	130%	95%	No

The key is to statistically measure the bias. To establish that a forecast is biased, you have to prove that the net bias is statistically significant using standard confidence intervals.

Type 2 Bias



- Ø This bias is a manifestation of business process specific to the product.
- Ø This can either be an over-forecasting or under-forecasting bias. This bias is hard to control, unless the underlying business process itself is restructured.
- Ø Examples:
 - Items specific to a few customers
 - Persistent demand trend when forecast adjustments are slow to respond to such trends
 - Distribution changes of an item over time
 - Either item getting distribution across new customers over time or
 - Item slowly going through an attrition with delistments over time.

Bias – Is there a remedy?



- Ø If bias is type 1, correcting the forecast is easy but making the organization adjust to unbiased forecasting is the harder sell.
 - Since Arithmetic accuracy conveys similar information as absolute accuracy, using a mass counter-adjustment is the easiest solution.
 - In Case 1, slashing the forecast across the board by 33% would dramatically increase the accuracy.
- Ø If bias is type 2
 - Each item bias needs to be examined for specific process reasons.
 - Process needs to be re-adjusted

Cut forecast by 33% in Case 1



	Original Forecast	Rev. forecast	Actual	Abs. Error	Pct. Error	Accuracy
Sku A	3	2.01	1	1	101%	0%
Sku B	50	33.5	25	9	34%	66%
Sku X	75	50.25	25	25	101%	0%
Sku Y	75	50.25	74	24	32%	68%
Sku Z	100	67	75	8	11%	89%
Total	303	203.01	200	66.51	33%	67%
Average	60.6	40.602	40	13.302		
	Absolute Accuracy				67%	
	Arithmetic Accuracy				99%	

Industry Benchmark Measurement



- Ø We measure item level absolute accuracy using an one-month bucket and a three-month bucket.
- Ø The one-month accuracy is measured using a two-month lag forecast ie. May actuals measured using March forecast
- Ø The three-month accuracy is measured using an one-month lag forecast ie. May-July actuals using April forecast.
- Ø Business policy issue
 - Quarter close effects
 - Unannounced business deals
- Ø The above have an effect on one-month accuracy but NOT on three-month accuracy.



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SAFETY STOCK

- Ø Why do we need safety stock?
- Ø Is safety stock related to Forecast Accuracy?
- Ø How do you calculate safety stock levels?

Safety stock



∅ Safety stock is defined

- as the component of total inventory needed to cover unanticipated fluctuation in demand or supply or both
- As the inventory needed to defend against a forecast error

∅ Hence Forecast error is a key driver of safety stock strategies.

Safety Stock Calculation



Ø Using all three determinants of Safety stock,

- $SS = SL * \text{Forecast Error} * \sqrt{\text{Lead Time}}$

Ø SL is Customer Service Level

- Generally set at 98% (why?)
- Which translates into a multiple of 2.054 (why?)

Ø Forecast Error used is the Root Mean Squared Error

Ø Lead time is either weeks or months, consistent with the forecast measurement period.

Importance of Forecast Error



Ø Lead times are externally determined

- Supplier Considerations
- Structure of your Supply Chain

Ø Service Level Targets are typically in a narrow band between 95% and 99.5%

Ø Hence Forecast Error is the big driver of safety stock.

Example



		Sku X	Sku Y	Sku Z
Lead Time	Months	0.75	2	2
Service Level	98%	2.054	2.054	2.054
Forecast Error	Monthly	16	11	5
Safety Stock	Units	28	32	15

Forecast Bias



- Ø Does Bias affect Safety stock?
 - Depends on whether it is type 1 or type 2 bias.
 - If bias can be quantified, then there is no uncertainty and hence no need for additional safety stock
- Ø If this is a type 1 bias, adjustment is easy
 - Add or subtract the bias to the forecasted quantity to arrive at your supply
 - Safety stock needs to be adjusted down to match the error contributed by the bias



ABOUT US

- Ø Who is the author?
- Ø What is Demand Planning LLC?
- Ø Who are Demand Planning LLC clients?
- Ø How can you contact the author of this paper?

About The Author



Dr. Mark Chockalingam is Founder and Managing Principal, Demand Planning LLC, a Business Process and Strategy Consultancy firm. He has conducted numerous training and strategy facilitation workshops in the US and abroad, and has worked with a variety of clients from Fortune 500 companies such as Wyeth, Miller SAB, FMC, Teva to small and medium size companies such as Au Bon pain, Multy Industries, Ticona- a division of Celanese AG.

Prior to establishing his consulting practice, Mark has held important supply chain positions with several manufacturing companies. He was Director of Market Analysis and Demand Planning for the Gillette Company (now part of P&G), and prior to that he led the Sun care, Foot care and OTC forecasting processes for Schering-Plough Consumer HealthCare.

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About Demand Planning LLC



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